## Ma

KEY STAGE 3

ALL TIERS

## Mathematics tests

## Mark scheme

 for Paper 2Tiers 3-5, 4-6, 5-7 and 6-8


National curriculum assessments

## Introduction

The test papers will be marked by external markers. The markers will follow the mark scheme in this booklet, which is provided here to inform teachers.

This booklet contains the mark scheme for paper 2 at all tiers. The paper 1 mark scheme is printed in a separate booklet. Questions have been given names so that each one has a unique identifier irrespective of tier.

## The structure of the mark schemes

The marking information for questions is set out in the form of tables, which start on page 11 of this booklet. The columns on the left-hand side of each table provide a quick reference to the tier, question number, question part and the total number of marks available for that question part.

The Correct response column usually includes two types of information:

- a statement of the requirements for the award of each mark, with an indication of whether credit can be given for correct working, and whether the marks are independent or cumulative
- examples of some different types of correct response, including the most common.

The Additional guidance column indicates alternative acceptable responses, and provides details of specific types of response that are unacceptable. Other guidance, such as when 'follow-through' is allowed, is provided as necessary.

Questions with a $U A M$ element are identified in the mark scheme by an encircled $U$ with a number that indicates the significance of using and applying mathematics in answering the question. The $U$ number can be any whole number from 1 to the number of marks in the question.

For graphical and diagrammatic responses, including those in which judgements on accuracy are required, marking overlays have been provided as the centre pages of this booklet.

The 2008 key stage 3 mathematics tests and mark schemes were developed by the Test Development Team at Edexcel.

## General guidance

## Using the mark schemes

Answers that are numerically equivalent or algebraically equivalent are acceptable unless the mark scheme states otherwise.

In order to ensure consistency of marking, the most frequent procedural queries are listed on the following two pages with the prescribed correct action. This is followed by further guidance relating specifically to the marking of questions that involve money, negative numbers, algebra, time, coordinates or probability. Unless otherwise specified in the mark scheme, markers should apply the following guidelines in all cases.

What if ...
$\left.\begin{array}{|r|l|}\hline \begin{array}{r}\text { The pupil's response } \\ \text { does not match } \\ \text { closely any of the } \\ \text { examples given. }\end{array} & \begin{array}{l}\text { Markers should use their judgement in deciding whether the response } \\ \text { corresponds with the statement of requirements given in the Correct response } \\ \text { column. Refer also to the Additional guidance. }\end{array} \\ \hline \begin{array}{r}\text { The pupil has } \\ \text { responded in a } \\ \text { non-standard way. }\end{array} & \begin{array}{l}\text { Calculations, formulae and written responses do not have to be set out in } \\ \text { any particular format. Pupils may provide evidence in any form as long as its } \\ \text { meaning can be understood. Diagrams, symbols or words are acceptable for } \\ \text { explanations or for indicating a response. Any correct method of setting out } \\ \text { working, however idiosyncratic, is acceptable. Provided there is no ambiguity, } \\ \text { condone the continental practice of using a comma for a decimal point. }\end{array} \\ \hline \text { The pupil has made a } \\ \text { conceptual error. }\end{array} \begin{array}{l}\text { In some questions, a method mark is available provided the pupil has made } \\ \text { a computational, rather than conceptual, error. A computational error is } \\ \text { a 'slip' such as writing 4 } \times 6=18 \text { in an otherwise correct long multiplication. } \\ \text { A conceptual error is a more serious misunderstanding of the relevant } \\ \text { mathematics; when such an error is seen, no method marks may be awarded. } \\ \text { Examples of conceptual errors are: misunderstanding of place value, such as } \\ \text { multiplying by 2 rather than 20 when calculating 35 × 27; subtracting the } \\ \text { smaller value from the larger in calculations such as 45 - 26 to give the } \\ \text { answer 21; incorrect signs when working with negative numbers. }\end{array}\right\}$

## What if ...

| The final answer is wrong but the correct answer is shown in the working. | Where appropriate, detailed guidance will be given in the mark scheme and must be adhered to. If no guidance is given, markers will need to examine each case to decide whether: |
| :---: | :---: |
|  | - the incorrect answer is due to a transcription error $\quad$ If so, award the mark. |
|  | - in questions not testing accuracy, the correct <br> answer has been given but then rounded or <br> truncated$\quad$ If so, award the mark. |
|  | - the pupil has continued to give redundant extra  <br> working which does not contradict work already <br> done If so, award the mark. |
|  | - the pupil has continued, in the same part of the question, to give redundant extra working which does contradict work already done. <br> If so, do not award the mark. Where a question part carries more than one mark, only the final mark should be withheld. |
| The pupil's answer is correct but the wrong working is seen. | A correct response should always be marked as correct unless the mark scheme states otherwise. |
| The correct response has been crossed or rubbed out and not replaced. | Mark, according to the mark scheme, any legible crossed or rubbed out work that has not been replaced. |
| More than one answer is given. | If all answers given are correct or a range of answers is given, all of which are correct, the mark should be awarded unless prohibited by the mark scheme. If both correct and incorrect responses are given, no mark should be awarded. |
| The answer is correct but, in a later part of the question, the pupil has contradicted this response. | A mark given for one part should not be disallowed for working or answers given in a different part, unless the mark scheme specifically states otherwise. |

## Marking specific types of question

Responses involving money
For example: £3.20 £7

| Accept $\checkmark$ | Do not accept $\boldsymbol{x}$ |
| :---: | :---: | :---: |

Responses involving negative numbers
For example: -2

| Accept $\checkmark$ | Do not accept $\boldsymbol{x}$ |
| :--- | :--- |
| To avoid penalising the error below <br> more than once within each question, <br> do not award the mark for the first <br> occurrence of the error wwithin each <br> question. Where a question part <br> carries more than one mark, olly <br> the final mark should be withheld. |  |
|  |  |


| Responses involving the use of algebra |  |
| :---: | :---: |
| For example: $2+n \quad n+2 \quad 2 n$ | $n^{2}$ |
| Accept $\checkmark$ | Take care ! Do not accept $\times$ |
| $\checkmark$ Unambiguous use of a different case or variable <br> eg $N$ used for $n$ $x$ used for $n$ | ! Unconventional notation $\text { eg } \begin{aligned} & n \times 2 \text { or } 2 \times n \text { or } n 2 \\ & \text { or } n+n \text { for } 2 n \\ & n \times n \text { for } n^{2} \\ & n \div 2 \text { for } \frac{n}{2} \text { or } \frac{1}{2} n \\ & 2+1 n \text { for } 2+n \\ & 2+0 n \text { for } 2 \end{aligned}$ <br> Within a question that demands simplification, do not accept as part of a final answer involving algebra. Accept within a method when awarding partial credit, or within an explanation or general working. <br> $\times$ Embedded values given when solving equations <br> eg in solving $3 x+2=32$, $3 \times 10+2=32 \text { for } x=10$ <br> To avoid penalising the two types of error below more than once within each question, do not award the mark for the first occurrence of each type within each question. Where a question part carries more than one mark, only the final mark should be withheld. |
| $\checkmark$ Words used to precede or follow equations or expressions <br> eg $t=n+2$ tiles or tiles $=t=n+2$ for $t=n+2$ | ! Words or units used within equations or expressions <br> eg $n$ tiles +2 $n \mathrm{~cm}+2$ <br> Do not accept on their own. Ignore if accompanying an acceptable response. |
| $\checkmark$ Unambiguous letters used to indicate expressions <br> eg $t=n+2$ for $n+2$ | $\mathbf{x}$ Ambiguous letters used to indicate expressions <br> eg $n=n+2$ for $n+2$ |


| Responses involving time <br> A time interval For example: 2 hours 30 minutes |  |
| :---: | :---: |
| Accept $\checkmark$ | Take care ! Do not accept $\times$ |
| $\checkmark$ Any unambiguous indication eg 2.5 (hours), 2h 30 <br> $\checkmark$ Digital electronic time ie 2:30 | x Incorrect or ambiguous time interval <br> eg 2.3(h), 2.30, 2-30, 2h 3, <br> 2.30 min <br> ! The unit, hours and/or minutes, is usually printed in the answer space. Where the pupil writes an answer outside the answer space, or crosses out the given unit, accept answers with correct units, unless the question has specifically asked for other units to be used. |
| A specific time For example: 8:40am | 17:20 |
| Accept $\checkmark$ | Do not accept $x$ |
| $\checkmark$ Any unambiguous, correct indication eg $08.40,8.40,8: 40,0840,840$, 8-40, twenty to nine, 8,40 <br> $\checkmark$ Unambiguous change to 12 or 24 hour clock <br> eg 17:20 as $5: 20 \mathrm{pm}, 17: 20 \mathrm{pm}$ | x Incorrect time <br> eg $\quad 8.4 \mathrm{am}, 8.40 \mathrm{pm}$ <br> X Incorrect placement of separators, <br> spaces, etc or incorrect use or omission of 0 <br> eg 840, 8:4:0, 084, 84 |

Responses involving coordinates
For example: (5,7)

| Accept $\checkmark$ | Do not accept $x$ |
| :---: | :---: |
| $\checkmark$ Unconventional notation eg ( 05,07 ) ( five, seven ) $\left(\begin{array}{l}x \\ (5, \\ 7 \\ 7\end{array}\right)$ $(x=5, y=7)$ | x Incorrect or ambiguous notation <br> eg $(7,5)$ <br> $\left(\begin{array}{ll}y & x \\ 7 & 5\end{array}\right)$ <br> ( $5 x, 7 y$ ) <br> $\left(5^{x}, 7^{y}\right)$ <br> $(x-5, y-7)$ |

## Responses involving probability

A numerical probability should be expressed as a decimal, fraction or percentage only.
$\begin{array}{llll}\text { For example: } & 0.7 & \frac{7}{10} \quad 70 \%\end{array}$

| Accept $\checkmark$ | Take care ! Do not accept x |
| :---: | :---: |
| $\checkmark$ Equivalent decimals, fractions and percentages eg $0.700, \frac{70}{100}, \frac{35}{50}, 70.0 \%$ | The first four categories of error below should be ignored if accompanied by an acceptable response, but should not be accepted on their own. However, to avoid penalising the first three types of error below more than once within each question, do not award the mark for the first occurrence of each type of error unaccompanied by an acceptable response. Where a question part carries more than one mark, only the final mark should be withheld. |
| $\checkmark$ A probability correctly expressed in one acceptable form which is then incorrectly converted, but is still less than 1 and greater than 0 <br> eg $\quad \frac{70}{100}=\frac{18}{25}$ | ! A probability that is incorrectly expressed <br> eg 7 in 10 <br> 7 over 10 <br> 7 out of 10 <br> 7 from 10 |
|  | ! A probability expressed as a percentage without a percentage sign. |
|  | ! A fraction with other than integers in the numerator and/or denominator. |
|  | A probability expressed as a ratio eg $7: 10,7: 3,7$ to 10 |
|  | x A probability greater than 1 or less than 0 |

## Recording marks awarded on the test paper

All questions, even those not attempted by the pupil, will be marked, with a 1 or a 0 entered in each marking space. Where 2 m can be split into 1 m gained and 1 m lost, with no explicit order, then this will be recorded by the marker as 1

The total marks awarded for a double page will be written in the box at the bottom of the right-hand page, and the total number of marks obtained on the paper will be recorded on the front of the test paper.

A total of 120 marks is available in each of tiers 3-5, 4-6, 5-7 and 6-8.

## Awarding levels

The sum of the marks gained on paper 1, paper 2 and the mental mathematics paper determines the level awarded. Level threshold tables, which show the mark ranges for the award of different levels, will be available on the NAA website www.naa.org.uk/tests from Monday 23 June 2008.






| Tier \& Question |  |  |  |  |  |  | k |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\|5 | 5-7 6-8 |  |  |  |  |  |
| 6 |  |  |  |  |  | Correct response | Additional guidance |
| a |  |  | 11 |  | 8 |  |  |
| b |  |  | 1n |  | 7 |  |  |
| c |  |  | 11 |  | 5 |  |  |



| Tier \& Question |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\| | 5-7 | 6-8 |  |  |  |  |
| 8 |  |  |  |  |  | Correct response | Additional guidance |
| a |  |  |  | 1 m | 2134 |  |  |
| b |  |  |  | 1 m | 663768 |  |  |


| Tier \& Question |  |  |  | Time machine |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 |  | 6-8 |  |  |  |
| 9 | 1 |  |  |  | Correct response | Additional guidance |
|  |  |  |  | $\begin{gathered} 2 \mathrm{~m} \\ \text { or } \\ 1 \mathrm{~m} \end{gathered}$ | 6 <br> Shows the value 94 or the values 4 and 2 or <br> Shows a complete correct method with not more than one computational error eg <br> - 100-46-48 <br> - $100-(46+48)$ <br> - $100-46=53$ (error) <br> $53-48=5$ | $\times$ For 1m, necessary brackets omitted eg $\cdot 100-46+48$ |


| Tier \& Question |  |  |  |  |  | Four cards |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6 | 6-8 |  |  |  |
|  | 2 |  |  |  | Correct response | Additional guidance |
|  |  |  |  | 2m <br> or <br> 1m | Matches all four statements to their correct positions, ie <br> Matches any two statements to their correct positions | ! Statement matched to more than one position <br> For 2 m or 1 m , do not accept as a correct match |




| Tier \& Question |  |  |  |  |  |  | Shopping |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |  |
| 13 | 5 |  |  |  |  | Correct response | Additional guidance |
| a | a |  |  | 1 m | $£ 1.15$ |  |  |
| b | b |  |  | 1 m | 5 |  | ! Reference to remainder <br> Condone reference to the correct amount of money left over <br> eg, accept <br> - 5 with 20 p change <br> - 5 r 20 <br> eg, do not accept <br> - $5.5(\ldots)$ or 5.6 <br> - 5 with 55 p change |


| Tier \& Question |  |  |  |  |  | Speedometer |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 14 | 6 |  |  |  | Correct response | Additional guidance |
| a | a |  |  | 1m | Indicates the correct value on the scale, ie | ! Inaccurate indication <br> Accept provided their marker would touch the circumference of the dial within 2 mm of the correct position, if extended |
| b | b |  |  | 1 m | 40 |  |



| Tier \& Question |  |  |  |  |  |  | Jug |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6-8 | 6-8 |  |  |  |  |
| 16 | 8 |  |  |  | Correct response | Additional guidance |  |
|  |  |  |  | 1 m | 750 |  |  |
|  |  |  |  | 1m | 100 |  |  |
|  |  |  |  | 1m | $\frac{1}{5}$ or equivalent fraction or decimal |  |  |


| Tier \& Question |  |  | Double shape |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 |  | 5-7 6-8 |  |  |  |
| 17 | 9 |  |  | Correct response | Additional guidance |
| a | a |  | 1m | Indicates Yes <br> and <br> gives a correct explanation <br> The most common correct explanations: <br> Show or imply the correct areas eg <br> - The area of the rectangle is 18 , the area of the square is 9 and $9 \times 2=18$ <br> - A is 18 and B is $18 \div 2=9$ <br> Refer to the space taken up by each shape eg <br> - Two of the squares can fit inside the rectangle <br> - If you draw a line down the middle of the rectangle, you get two of the squares <br> - A holds twice as many squares as B <br> Refer to the ratio of lengths together with the equal widths eg <br> - They are the same width but the rectangle is twice as long as the square <br> - $6 \times 3$ is twice $3 \times 3$ | ! Incorrect units <br> Condone <br> eg, accept <br> - $18 \mathrm{~cm}, 9 \mathrm{~cm}$ <br> - $18^{2}, 9^{2}$ <br> $\checkmark$ Minimally acceptable explanation <br> eg <br> - 18,9 <br> - $2 \times 9$ (or double 9 ), 9 <br> - $18,18 \div 2$ <br> $\times$ Incomplete explanation <br> eg <br> - The area of the rectangle is 18 <br> $\checkmark$ Minimally acceptable explanation <br> eg <br> - A holds two squares <br> - You cut A in half to get B <br> - Rectangle divided into two squares on the diagram <br> - I counted the squares inside the shapes <br> $\times$ Incomplete explanation <br> eg <br> - The area of A is twice the area of B <br> - B is half of A <br> - He's just added another shape on <br> - I counted the squares <br> $\checkmark$ Minimally acceptable explanation <br> eg <br> - Equal width, but the length is doubled <br> - Same height, but width is twice as long <br> - $6 \times 3,3 \times 3$ <br> $\times$ Incomplete explanation <br> eg <br> - The rectangle is twice as long as the square <br> - Because $A$ is 6 squares long and $B$ is 3 squares long |




| Tier \& Question |  |  |  |  |  | Track |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
| 19 | 11 | 2 |  |  | Correct response | Additional guidance |
| a | a | a |  | 1m | 5 | ! Response assumes the piece of track shown has already been counted For answers of 4 for part (a) followed by 5 for part (b), mark as 0,1 |
| b | b | b |  | 1m | 6 |  |


| Tier \& Question |  |  |  |  |  |  | Matching expressions |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6 |  |  |  |  |  |
| 20 | 12 | 3 |  |  | Correct response |  | Additional guidance |
|  |  |  |  | 2m <br> or <br> 1m | Matches all four statements correctly, ie <br> Matches three of the statements correctly | ! | Statement matched to more than one expression For 2 m or 1 m , do not accept as a correct match |


| Tier \& Question |  |  |  |  |  |  | Area |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |  |
| 21 | 13 | 4 |  |  | Correct response | Additional guidance |  |
|  |  |  |  | 1 m | Gives both correct areas, ie 9 then 3 |  |  |


| Tier \& Question |  |  |  |  |  | Values |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\| |  | -7-8 |  |  |  |
| 22 | 14 | 5 |  |  | Correct response | Additional guidance |
| a | a | a |  | 1 m | 6 | ! Incomplete processing Penalise only the first occurrence eg, for parts (a) and (b) |
| b | b | b |  | 1m | -2 | $4-6$ <br> Mark as 0,1 |





| Tier \& Question |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 |  | 5-7 |  |  |  |  |
| 26 | 16 | 9 |  |  | Correct response | Additional guidance |
| a | a | a |  | 1m <br> 1m <br> U1 | Gives a pair of prime numbers that sum to 16 , ie <br> 3 and 13, in either order <br> or <br> 5 and 11, in either order <br> Gives a different pair of prime numbers that sum to 16 from any credited for the first mark | $\times$ Values credited for the first mark repeated but in reverse order |
| b | b | b |  | 1m <br> (U1) | Completes the sentence correctly, giving an even number greater than 16 and a correct pair of prime numbers that sum to their number eg <br> - ... even number 20 ... <br> ... prime numbers 7 and 13 <br> - ... even number 22 ... <br> ... prime numbers 11 and 11 <br> - ... even number 50 ... <br> ... prime numbers 3 and 47 | $\times$ Their even number is less than or equal to 16 <br> Markers may find the following values useful: |


| Tier \& Question |  |  |  |  | Side length |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 |  | 5-7 6 | 6-8 |  |  |
| 27 | 19 | 10 |  | Correct response | Additional guidance |
|  |  |  |  | 6.3 or equivalent <br> Shows the value 25.2 or equivalent <br> or <br> Shows a complete correct method with not more than one computational error eg <br> - $8.4 \times 3 \div 4$ <br> - $(8.4+8.4+8.4) \div 4$ <br> - $8.4+8.4+8.4=25.6$ (error), <br> $25.6 \div 4=6.4$ | $\times$ For 1m, necessary brackets omitted eg $\text { - } 8.4+8.4+8.4 \div 4$ |



| Tier \& Question |  |  |  |  |  |  | Darts |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5 | 5-7 | 6-8 |  |  |  |  |
|  | 21 | 12 | 2 |  | Correct response | Additional guidance |  |
|  |  |  |  | 1 m | Gives all three correct numbers, ie 10,15 and 20 [any order] |  |  |



| Tier \& Question |  |  |  |  | Concorde |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 4-6 | 5-7 6 |  |  |  |  |
| 23 | 14 | 4 |  | Correct response | Additional guidance |
|  |  |  | $2 \mathrm{~m}$ <br> or <br> 1m | Shows or implies a correct rate, other than 1 mile every 3 seconds, even if it doesn't use single units of time eg <br> - 20 (miles) per minute <br> - $\frac{1}{3}$ (mile) in a sec <br> - 10 miles in 30 seconds <br> - 60 miles every 3 mins <br> or <br> Shows or implies a complete correct method with not more than one computational or rounding error eg <br> - $20 \times 60$ <br> - $\frac{60}{3} \times 60$ <br> - $\frac{1}{3} \times 3600$ <br> - $1 \div 3=0.33$ (premature rounding) $0.33 \times 60^{2}=1188$ | ! For 1m, unit(s) abbreviated Condone provided unambiguous within the context of the question eg, for 1 m accept <br> - 20 m per min <br> - $\frac{1}{3} \mathrm{~m} / \mathrm{s}$ [miles implied by given context] eg, for 1 m do not accept <br> - 20 m per m [ambiguity between miles and minutes] |


| Tier \& Question |  |  |  |  |  | Counters in a bag |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 5-7 6-8 | 6-8 |  |  |  |
|  | 24 | 15 | 5 |  | Correct response | Additional guidance |
|  |  |  |  | 2m <br> or <br> 1m | Completes the sentence correctly with three positive integers $r, w$ then $y$, such that $w=2 r$ and $y<r$ <br> eg <br> - 2, 4 then 1 <br> - 3, 6 then 1 or 2 <br> - 4,8 then 1,2 or 3 <br> Completes the sentence with three integers $r, w$ then $y$, such that $w=2 r$ and $y=0$ eg <br> - 2, 4 then 0 <br> - 3, 6 then 0 <br> or <br> Completes the sentence with three values $r, w$ then $y$ between zero and one, such that $r>\frac{1}{4}, w=2 r$ and $r+w+y=1$ <br> eg <br> - $\frac{2}{7}, \frac{4}{7}$ then $\frac{1}{7}$ <br> - $0.3,0.6$ then 0.1 | $\times$ For 1m, values for $r$ or $w$ negative or zero eg <br> - $-1,-2$ then 0 <br> - 0,0 then 0 |


| Tier \& Question |  |  |  |  |  | Perimeters |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |
|  | 25 | 16 | 6 |  | Correct response | Additional guidance |
|  | a | a | a | 1m | $7 a+3$ | ! Unsimplified expression or unconventional notation eg <br> - $\frac{42 a+18}{6}$ <br> - $(42 \times a+18) \div 6$ <br> Condone <br> x Necessary brackets omitted <br> eg <br> - $42 a+18 \div 6$ |
|  | b | b | b | 1m | 5 |  |
|  | c | c | c | 1 m | 24 | ! Units given <br> Ignore, even if incorrect for a perimeter <br> eg, accept <br> - 24 cm <br> - $24 \mathrm{~cm}^{2}$ <br> $\times$ Incomplete processing <br> eg <br> - $4 \times 6$ |



| Tier \& Question |  |  |  |  |  |  | Lawn |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $3-5$ $4-6$ $5-7$ $6-8$ <br>  27 18  |  |  |  |  |  |  |  |
|  | 27 | 18 | 8 |  | Correct response | Additional guidance |  |
|  |  |  |  | $2 \mathrm{~m}$ <br> or $1 \mathrm{~m}$ | 28.(...) or $9 \pi$ <br> Shows or implies a complete correct method for finding the area of the lawn, with no evidence of conceptual error and not more than one computational or rounding error eg <br> - Shows the digits $282(\ldots$ ) or 283 <br> - $3^{2} \times \pi$ <br> - $\pi=3$ (rounding error), $9 \times 3=27$ | $\times$ For 1m, conceptual error <br> eg <br> - $3^{2} \times \pi=19$ or $18.8(\ldots)$ or $6 \pi$ <br> - $\pi 3^{2}=89$ <br> - Area $=2 \times 3 \times \pi$ |  |


| Tier \& Question |  |  |  |  |  |  | Triangular numbers |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 | 6-8 |  |  |  |  |
|  | 28 | 19 | 9 |  |  | Correct response | Additional guidance |
|  | a | a | a | 1 m | 55 |  |  |
|  | b | b | b | 1 m | 5050 |  |  |




| Tier \& Question |  |  | Special offer |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 5-7 | 6-8 |  |  |  |
|  | 22 | 12 |  | Correct response | Additional guidance |
|  |  |  | $2 \mathrm{~m}$ <br> or 1m <br> U1 | Indicates Both paid the same and gives a correct justification eg <br> - Marie paid $96-9.60=86.40$ <br> Richard paid $108-21.60=86.40$ <br> - $0.9 \times 96=86.4$ <br> $0.8 \times 108=86.4$ <br> Gives a correct justification but makes an incorrect or no decision <br> or <br> Gives a correct justification with not more than one computational or rounding error, but follows through to make their correct decision eg <br> - Marie paid $96-9.60=87.4(0)$ (error) <br> Richard paid $108-21.60=86.4(0)$ | $\checkmark$ For $2 m$, minimally acceptable justification eg <br> - 96 - 9.6(0), 108 - 21.6(0) <br> - $0.9 \times 96,0.8 \times 108$ <br> - 86.4(0) <br> $\times$ For $2 m$ or $1 m$, incomplete justification eg <br> - $10 \%$ off 96 is the same as $20 \%$ off 108 <br> - It works out to be the same <br> $\times$ For 1m, conceptual error <br> eg $\text { -20\% off } \begin{aligned} 108 & =108-(108 \div 20) \\ & =108-5.40 \\ & =102.60 \end{aligned}$ |


| Tier \& Question |  |  | Marking overlay available |  | Planes |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 6-7 | 6-8 |  |  |  |
|  | 23 | 13 |  | Correct response | Additional guidance |
|  | a | a | 1 m | Indicates the correlation is positive | ! Positive qualified <br> Ignore <br> eg, accept <br> - Strong positive <br> - Direct positive <br> $\times$ Sign of correlation not indicated <br> eg <br> - High <br> - Strong <br> ! Relationship quantified <br> Ignore alongside a correct response <br> $\times$ Relationship described without reference to correlation <br> eg <br> - The greater the wingspan, the more passengers it can hold |
|  | b | b | 1 m | Draws a line of best fit within the tolerance, and at least of the length, as shown on the overlay | ! Line not ruled or accurate <br> Accept provided the line is within tolerance, and at least of the length required <br> ! Line of best fit is incorrect beyond the dashed lines on the overlay Condone eg, accept <br> - A correct line of best fit that is then joined to the origin |
|  | c | c |  | 3600 to 5200 inclusive <br> Shows a value between 180 and 260 inclusive or <br> Shows a value that follows through from their line of best fit eg <br> - Their line passes through the point $(40,280)$, final answer: 5600 | ! For $1 m$, range for follow-through value If their line goes through $(40, y)$ accept follow-through as $20 \times(y \pm 10)$ provided their line always has a positive gradient |




| Tier \& Question |  |  |  |  | Shadows |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 5-7 |  |  |  |  |
|  | 26 | 16 |  | Correct response | Additional guidance |
|  |  |  | $2 \mathrm{~m}$ <br> or <br> 1m | 4.2 or equivalent <br> Shows the value $\frac{2}{3}$ or $\frac{3}{2}$ or equivalents <br> or <br> Shows or implies a complete correct method with not more than one computational or rounding error eg <br> - $1.8 \div 2.7 \times 6.3$ <br> - $1.8 \div 2.7=0.6$ (rounding error) $0.6 \times 6.3=3.78$ <br> - $6.3 \div 2.7=2.3$ (rounding error) $1.8 \times 2.3=4.14$ | ! For 1m, value rounded For $\frac{2}{3}$, accept $0.66(\ldots)$ or 0.67 |


| Tier \& Question |  |  |  |  |  | 1,2,4 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\| | 5-7 6 |  |  |  |  |  |
|  |  |  |  |  | Correct response | Additional guidance |  |
|  |  |  |  | 3 m <br> or <br> 2m <br> or <br> 1m | Gives a complete correct response that satisfies all four of the following conditions: <br> 1. Indicates that A is 8 <br> 2. Indicates that $B$ is 7 <br> 3. Indicates that C is 8 <br> 4. Shows or implies correct substitution at least for value C <br> eg <br> - $\frac{4\left(4^{2}-3 \times 4+8\right)}{6}$ <br> - $\frac{4 \times 12}{6}$ <br> - $48 \div 6$ <br> Gives a response that satisfies three of the four conditions <br> Gives a response that satisfies two of the four conditions |  |  |


| Tier \& Question |  |  | Triangles |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\|5-7 | 5-7 6-8 |  |  |  |
|  |  | 2818 |  | Correct response | Additional guidance |
|  |  | a | $2 \mathrm{~m}$ <br> or <br> 1m | $14.4(\ldots)$, or $4 \sqrt{ } 13$, or $\sqrt{ } 208$ <br> Shows a correct method that indicates at least the intention to square and subtract the two given lengths <br> eg <br> - $17^{2}-9^{2}$ <br> - 289-81 <br> - 208 seen | ! Value of 14 <br> Do not accept unless a correct method or a more accurate value is seen <br> $\times$ For $2 m$ or $1 m$, method uses accurate or scale drawing |
|  |  | b | $2 \mathrm{~m}$ <br> or $1 \mathrm{~m}$ | 7.8 or $7.79(\ldots)$ <br> Shows or implies a correct trigonometric ratio involving not more than one unknown eg <br> - Answer of 7.7 <br> - $12 \tan 33$ <br> - $\tan 33=\frac{\mathrm{DF}}{12}$ <br> - $\tan 33=0.6$ (premature rounding), $12 \times 0.6=7.2$ <br> - $\tan 57=\frac{12}{x}$ | ! Value of 8 <br> Do not accept unless a correct method or a more accurate value is seen <br> $\times$ For $2 m$ or $1 m$, method uses accurate or scale drawing <br> ! For 1m, no indication of which angle is being considered eg $\text { - } \tan =\frac{\mathrm{DF}}{12}$ <br> For 1 m , accept only if the trigonometric ratio is correct for the given angle DEF |


| Tier \& Question |  |  |  | Box plots |
| :---: | :---: | :---: | :---: | :---: |
| 3-5 4- | 5-7 6-8 |  |  |  |
|  | 19 |  | Correct response | Additional guidance |
|  | a | 1m | 6 |  |
|  | b | 1 m | Gives a correct justification eg <br> - Median for year $10=56$, Median for year $11=65$, $65-56=9$ <br> - The medians are the vertical lines inside the grey boxes, they are $4 \frac{1}{2}$ divisions apart and this is 9 marks since 1 division $=2$ marks | $\checkmark$ Minimally acceptable justification <br> eg <br> - 56, 65 <br> - The medians are the vertical lines inside the boxes and they are 9 marks apart <br> - There is a gap of 9 [with both medians indicated on the graph] <br> ! Ambiguous notation <br> eg $\text { - } 56-65$ <br> Condone <br> - Incomplete justification <br> eg <br> - The difference between the medians is 9 marks on the graph |
|  | c | 1 m | Indicates Yes <br> and <br> gives a correct explanation, referring to <br> the inter-quartile range <br> eg <br> - Inter-quartile range for year $10=33$, Inter-quartile range for year $11=18$, so year 11 was more consistent <br> - The middle half of the year group was less spread out for year 11 than for year 10 <br> - The grey box shows the inter-quartile range and it is shorter for year 11 | $\checkmark$ Minimally acceptable explanation eg <br> - 33, 18 <br> - Its inter-quartile range is 15 less <br> - The IQ range is smaller <br> - The IQ range is bigger for year 10 <br> - The box is shorter (or smaller) <br> - For Y10: 43 to 76, for Y11: 51 to 69 <br> - It is shorter [distance between upper and lower quartiles indicated on both box plots] <br> ! 'Inter-quartile range' referred to as 'range' within an otherwise correct explanation Accept only if it is clear the response actually refers to the inter-quartile range <br> eg, accept <br> - For year 10, range $=33$ <br> For year 11, range $=18$ <br> eg, do not accept <br> - The range is bigger for year 10 <br> $\times$ Incomplete explanation <br> eg <br> - Year 11 is shorter than year 10 <br> - The results for year 10 are more spread out than in year 11 |


| Tier \& Question |  |  | Circle graph |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6 | 5-7 6-8 |  |  |  |
|  |  | 20 |  | Correct response | Additional guidance |
|  |  | a | $2 \mathrm{~m}$ <br> or 1m | Completes both pairs of coordinates correctly, ie $(3,4)$ and $(3,-4)$, in either order <br> Completes either pair of coordinates correctly or <br> Shows the value 16 <br> or <br> Shows or implies a correct method for finding the value of $y$ <br> eg <br> - $y^{2}=25-3^{2}$ |  |
|  |  | b | 1 m | 5 | x -5 or $\pm 5$ |
|  |  | c | $2 \mathrm{~m}$ <br> or 1m | Gives P as $(3.5,3.5)$ <br> Shows the value $3.5(\ldots)$ or 12.5 or equivalent or <br> Shows or implies a correct method for finding the value of $x$ or $y$ <br> eg <br> - $2 y^{2}=25$ <br> - $x^{2}=25 \div 2$ | ! For $2 m$, gives $P$ as ( $-3.5,-3.5$ ) <br> Condone <br> $\times$ For $2 m$, equivalent fractions or decimals |


| Tier \& Question |  |  |  | Giant pandas |
| :---: | :---: | :---: | :---: | :---: |
| 3-5 4-6 | 5-7 6-8 |  |  |  |
|  | 21 |  | Correct response | Additional guidance |
|  |  | $2 \mathrm{~m}$ <br> or $1 \mathrm{~m}$ | Shows the digits $11(\ldots)$ <br> or <br> Shows or implies a complete correct method eg <br> - $1600 \div 140 \times 100$ <br> - $\frac{1600}{1.4}$ <br> - $\frac{160000}{140}$ | ! For $2 m$ upper bound used Since pupils could assume 1600 is given to the nearest 100 in the context of the question, accept use of upper bound provided a correct method is seen eg, for 2 m accept <br> - $1650 \div 140 \times 100$, answer: 1200 <br> $\checkmark$ For $1 m$, lower and/or upper bound used within a correct method eg , for 1 m accept <br> - $1650 \div 140 \times 100$ <br> - $1550 \div 1.4$ |


| Tier \& Question |  |  |  |  | Prism |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 3-5 | 4-6\|5 | 5-7 6-8 |  |  |  |
|  |  | 22 |  | Correct response | Additional guidance |
|  |  |  | $\begin{array}{\|c\|\|} \hline 3 \mathrm{~m} \\ \text { or } \\ 2 \mathrm{~m} \\ 2 \\ \\ \\ \\ \\ \text { or } \\ 1 \mathrm{~m} \\ \\ \text { U1 } \\ \\ \hline \end{array}$ | $6.9(\ldots)$, or $4 \sqrt{ } 3$, or $\sqrt{ } 48$ <br> Shows or implies a correct method with not more than one computational or rounding error eg <br> - $\sqrt{32+16}$ <br> - $\sqrt{ } 32=5.6$ (rounding error) $\mathrm{AC}^{2}=5.6^{2}+4^{2}$ $\mathrm{AC}=6.8(\ldots)$ <br> - $\sqrt{ } 32=6$ (premature rounding) $\sqrt{36+16}=7.2$ <br> Shows sufficient working to indicate correct application of Pythagoras' theorem for at least one triangle <br> eg <br> - $4^{2}+4^{2}$ <br> - $2 \times 16$ <br> - $5.6(\ldots)$ or 5.7 seen <br> - $(\text { Their } B C)^{2}+4^{2}$ | ! Value of 7 <br> Do not accept unless a correct method or a more accurate value is seen <br> $\times$ For $3 m, 2 m$ or $1 m$, method uses accurate or scale drawing |




| Tier |  |  |  | Question | Page |
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| Tier |  |  |  | Question | Page |
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